# Module 6: Logic circuits with DNA strand displacement (part 2) 

CSE590: Molecular programming and neural computation.

## Fluorescent reporters can be used to follow reaction kinetics



The sequences of inputs and outputs can be completely independent.

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Gate


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## Fluorescent reporters can be used to follow reaction kinetics

$$
\stackrel{2}{-3} \xrightarrow{\rightarrow} \quad 0-1 x
$$

Input/Analyte



In + Gate $\xrightarrow{\mathrm{k}}$ Out + Waste
(I0 nM gates, 30 nM readout, TAE $12.5 \mathrm{mM} \mathrm{Mg}{ }^{++}$)

## Toehold strength determines reaction rate

$$
\stackrel{1}{-} \xrightarrow{3} \rightarrow \quad 0-1 x
$$

Input/Analyte


Gate


## Competition and thresholding



## Competition and thresholding



## Competition and thresholding



## Amplification: An input can act catalytically and release multiple outputs

## Reaction mix



Gate


Fuel strand


Fuel strand

Qian and Winfree, Science (201I)
(see also Zhang et al. Science (2007), Seelig et al. JACS (2006), Turberfield et al. PRL (2004))

## Amplification: An input can act catalytically and release multiple outputs

Reaction mix


## Amplification: An input can act catalytically and release multiple outputs


$\xrightarrow{2}=-$

$\xrightarrow{2}-3$

## Amplification: An input can act catalytically and release multiple outputs


$\xrightarrow{2}=-$

$\xrightarrow{2} \stackrel{3}{-}$

## Amplification: An input can act catalytically and release multiple outputs



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## Amplification: An input can act catalytically and release multiple outputs

$$
\begin{array}{cc}
2 & 3 \\
2 & 3 \\
\hline
\end{array}
$$

$$
\begin{aligned}
& \stackrel{1}{2} \\
& \leftarrow_{I^{*}} \frac{2}{2^{*}} 3^{*} . \\
& \leftarrow_{1^{*}} \frac{2}{2^{*}} 3^{*}=
\end{aligned}
$$

## Amplification: An input can act catalytically and release multiple outputs



Qian and Winfree, Science (201I)
(see also Zhang et al. Science (2007), Seelig et al.JACS (2006),Turberfield et al. PRL (2004))

## Combining amplification and thresholding



Qian and Winfree, Science (201I)
(see also Zhang et al. Science (2007), Seelig et al.JACS (2006),Turberfield et al. PRL (2004))

## Combining amplification and thresholding





## Seesaw OR logic



## Seesaw AND logic



OFF: 0 ~ 0.2


ON: $0.8 \sim 1$

$0=0.1 \times 1=0.9 x \quad 1 x=100 n M$

Slide credit: Lulu Qian

## Logic gate cascades





$$
0=0.1 \times 1=0.9 x \quad 1 x=100 n M
$$

Slide credit: Lulu Qian

## Logic gate cascades






$$
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## Logic gate cascades



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## Multi input logic gates



## Multi output logic gates



## A four-bit square root circuit



Slide credit: Lulu Qian

## A four-bit square root circuit



Slide credit: Lulu Qian

## A four-bit square root circuit




$$
\cdots . y_{1}^{\mathrm{OFF}}-\mathrm{y}_{1}^{\mathrm{ON}} \quad \cdots \mathrm{y}_{2}^{\mathrm{OFF}}-\mathrm{y}_{2}^{\mathrm{ON}}
$$

$$
0=0.1 \times 1=0.9 x \quad 1 x=50 n M
$$

Slide credit: Lulu Qian

## A four-bit square root circuit



Slide credit: Lulu Qian

## Take home message so far

We can build simple logic gates and circuits using DNA. DNA strand displacement circuits are the largest engineered molecular circuits built so far. But they are still really small compared to electronic ciruits or biological gene regulatory networks.


## Differences and similarities between electronic and molecular circuits

## I. Lack of spatial isolation limits reusability and leads to crosstalk

2. Computation energy and non-reusable gates: Both inputs and gates are consumed as the circuit is evaluated by cascade reactions, so they cannot be reused.
3. Data encoding: Information is encoded in the sequences and concentration of biomolecules.
4. Lack of clear hardware software separation: Gates and circuits come preprogrammed for the specific computation they are meant to carry out.
5. Speed of computation: A circuits evaluation under typical reaction conditions takes minutes to hours.
6. Need for dual-rail logic: NOT is difficult to implement

## One way forward: spatially localized DNA circuits



## Strand displacement with DNA hairpins


input
Single-stranded DNA can bind to itself

## Strand displacement with DNA hairpins



## Strand displacement with DNA hairpins


hairpin transmission line

## Strand displacement with DNA hairpins


output remains attached
input and output have the same sequence

## Rows of DNA hairpins act as wires



## Rows of DNA hairpins act as wires



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hairpin transmission line

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## Rows of DNA hairpins act as wires



## Rows of DNA hairpins act as wires


hairpin transmission line

## Rows of DNA hairpins act as wires


hairpin transmission line

## Rows of DNA hairpins act as wires



## Rows of DNA hairpins act as wires

## fluorescent <br> reporter


hairpin transmission line

## Rows of DNA hairpins act as wires



## Rows of DNA hairpins act as wires

## fluorescent <br> reporter



## Rows of DNA hairpins act as wires

## fluorescent <br> reporter



## Rows of DNA hairpins act as wires

fluorescent
reporter


## Rows of DNA hairpins act as wires

fluorescent<br>reporter



## Rows of DNA hairpins act as wires



## Experimental validation

single spacing
double spacing




quadruple spacing
 15
triple spacing





Reaction conditions:
~10nM origami, 20nM probe, 200nM input, 200nM fuel

## Take-home message

We can propagate a signal in a controlled way using only a fixed number of sequences

| Wire of <br> length $\mathbf{n}$ | non- <br> localized | localized |
| :---: | :---: | :---: |
| Nbr of <br> domains | $2 n+1$ | 3 |



Localized OR gates


$$
\begin{aligned}
& H\left(A_{0}, Y\right)>H(X, Y) \\
& H\left(B_{0}, Y\right) \\
& \quad+F(Y, X)
\end{aligned}
$$

Friday, January 24, 14

## Localized adder circuits



## Take home message

Localization enables composability of DNA circuits


## Outlook and future work

I. Communication between multiple origami enables circuits scale-up

2. Testing circuits in live cells


## Summary

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## Summary

I. Circuits that can work in cells and other "wet" environments have interesting applications as therapeutics and diagnostics.
2. Synthetic DNA is an engineering material for the construction of nanoscale structures and circuits.
3. DNA strand displacement circuits are the largest rationally designed molecular circuits so far but size and reliability are limited by the need to make sequences of all components orthogonal.
4. Spatial isolation allows us to organize the flow of information in a better way and makes it much easier to design and compose large circuits.

